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Effects of Very Low Piston Speed Regimes on Near-Isothermal Behaviour of Piston Expanders for Micro-CAES Systems

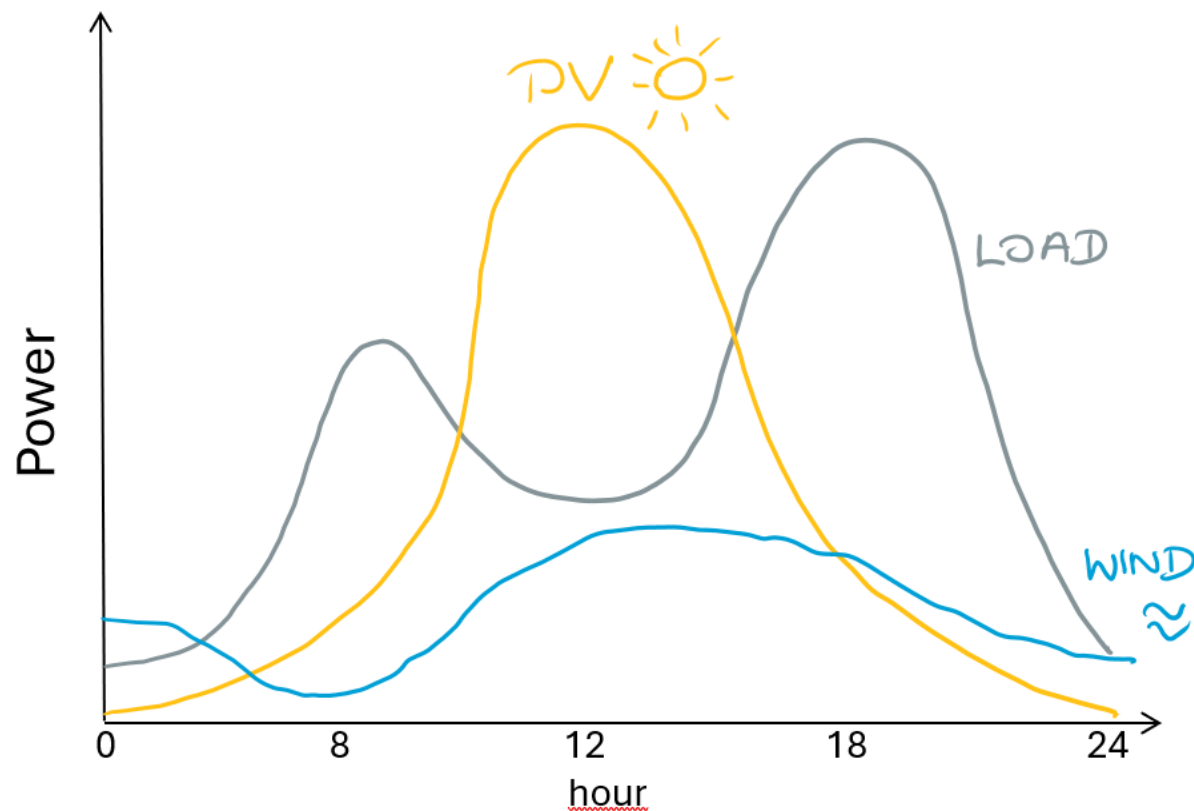
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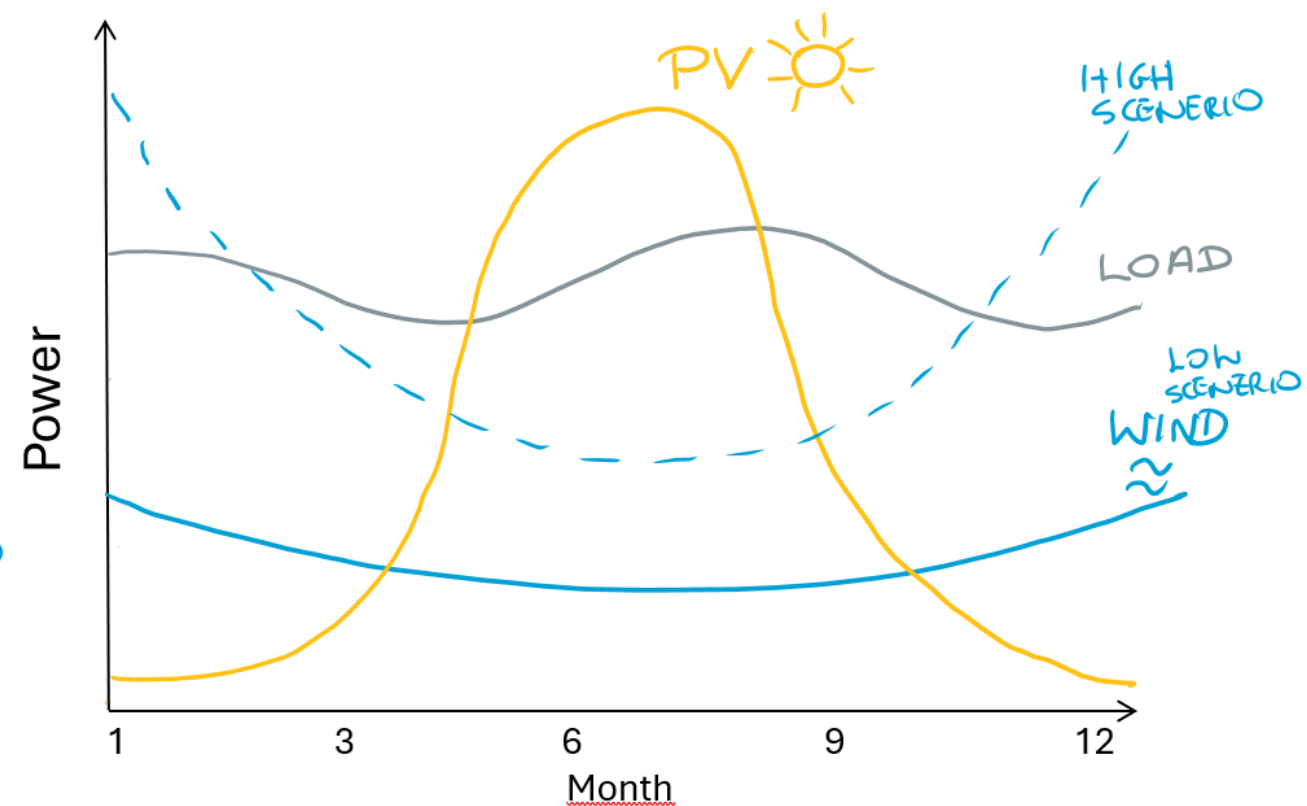
7th International Conference on Energy and Environment: bringing together Engineering and Economics
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Motivation

Daily

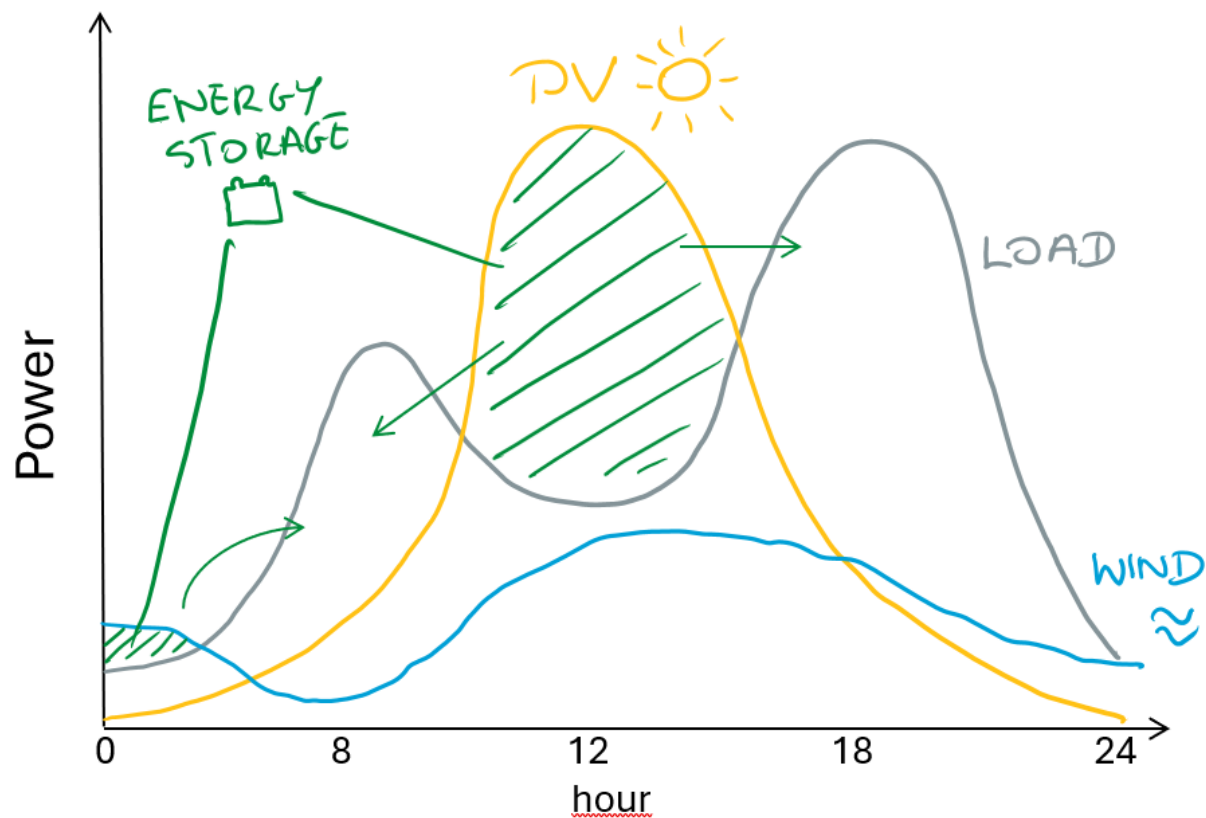


Yearly

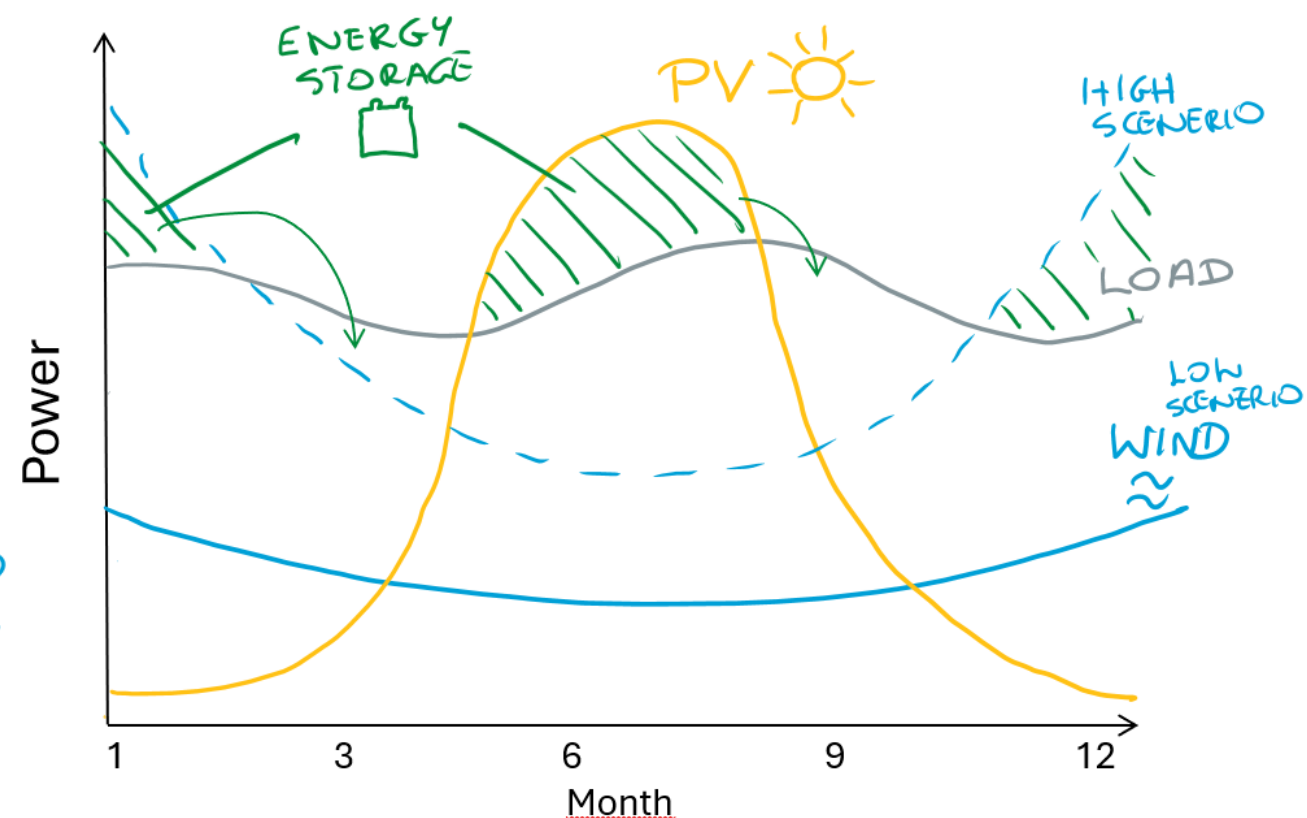


Motivation

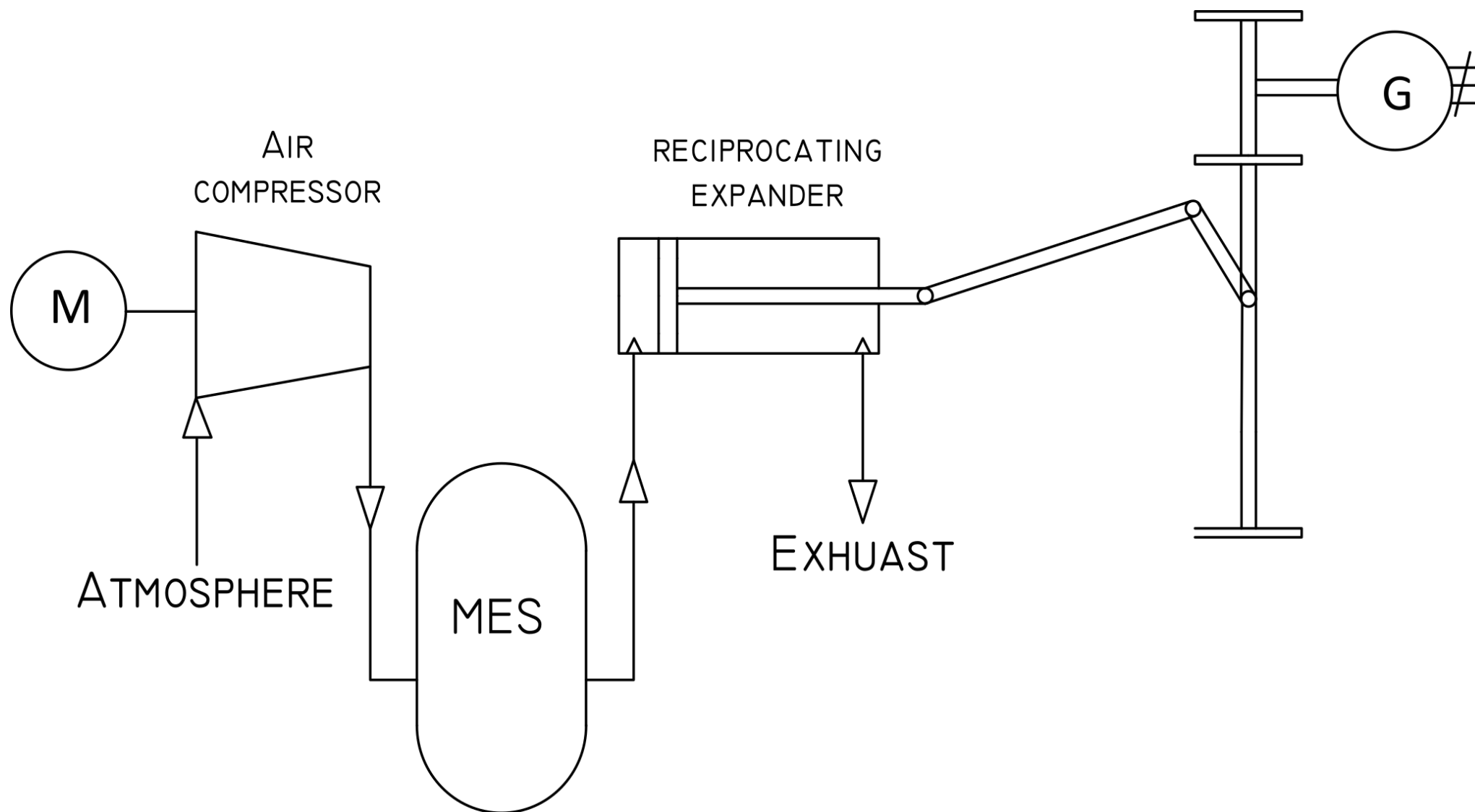
Daily



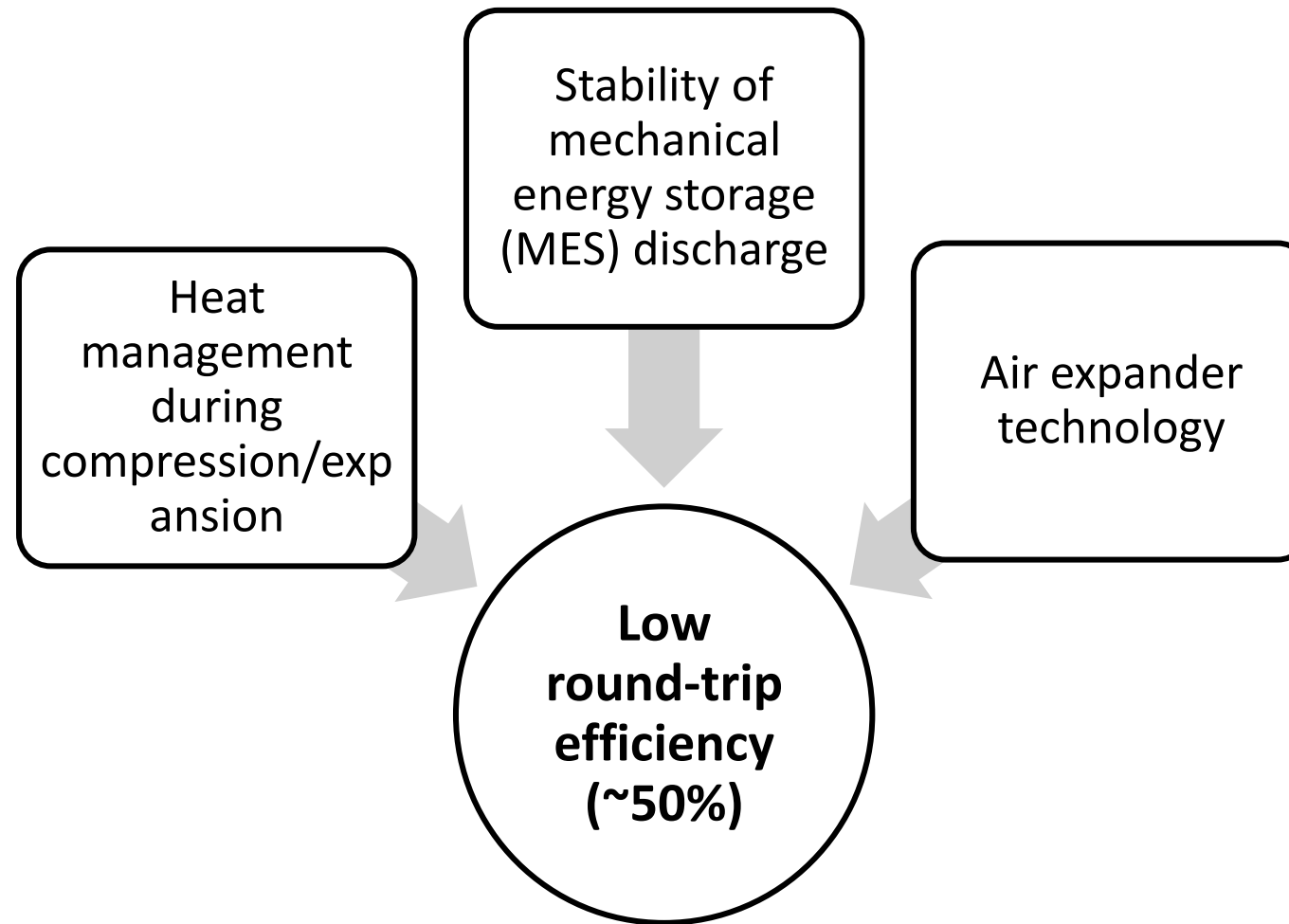
Yearly



Micro-CAES



Key barriers of CAES technology



Objective: Investigate the influence of piston speed on the polytropic exponent.

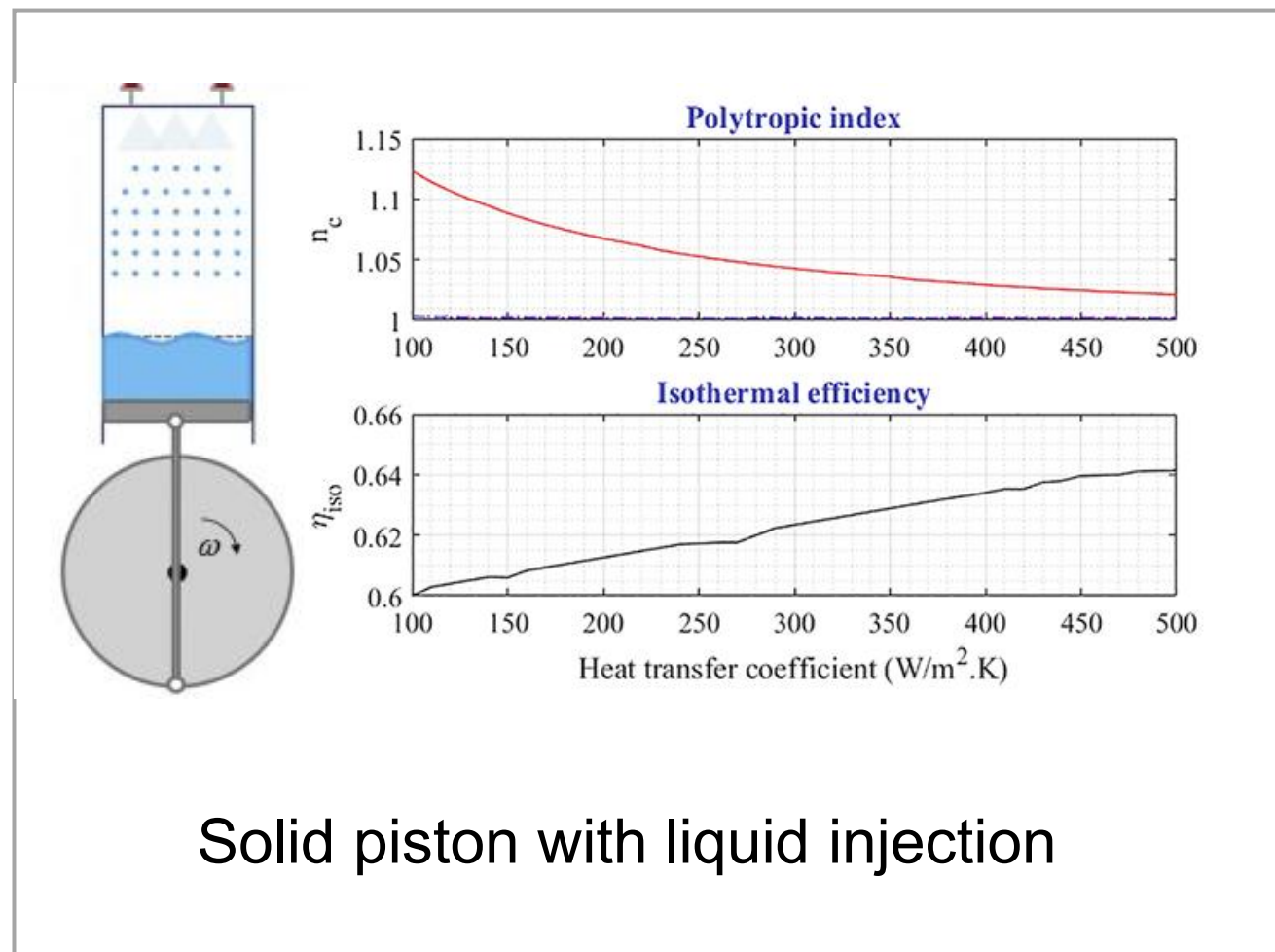
Hypothesis: Lower speeds increase heat transfer, shifting the process towards near-isothermal behavior.

*Maia, T. A. C., Barros, J. E. M., et al., Appl Energy 182 (2016) 358–364.

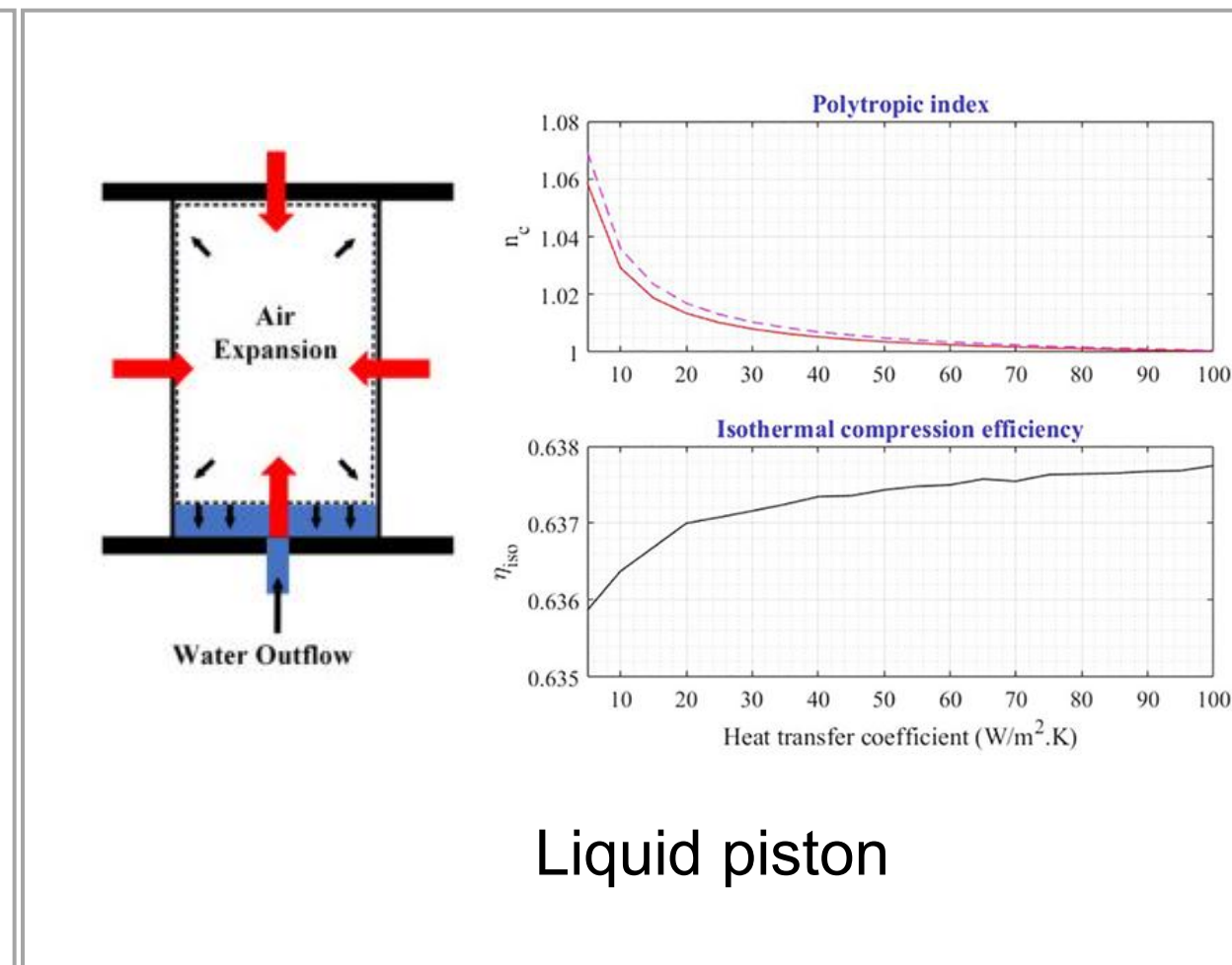
*He, W. and Wang, J., Renewable and Sustainable Energy Reviews 87 (2018) 77–95.

Existing approaches to improve heat transfer

Dib & Haberschill (2021) studied heat supply methods in expanders for energy storage.



Solid piston with liquid injection



Liquid piston

G. Dib and P. Haberschill, "Thermodynamic investigation of quasi-isothermal air compression/expansion for energy storage," Energy Conversion and Management, vol. 235, 114027, May 2021.

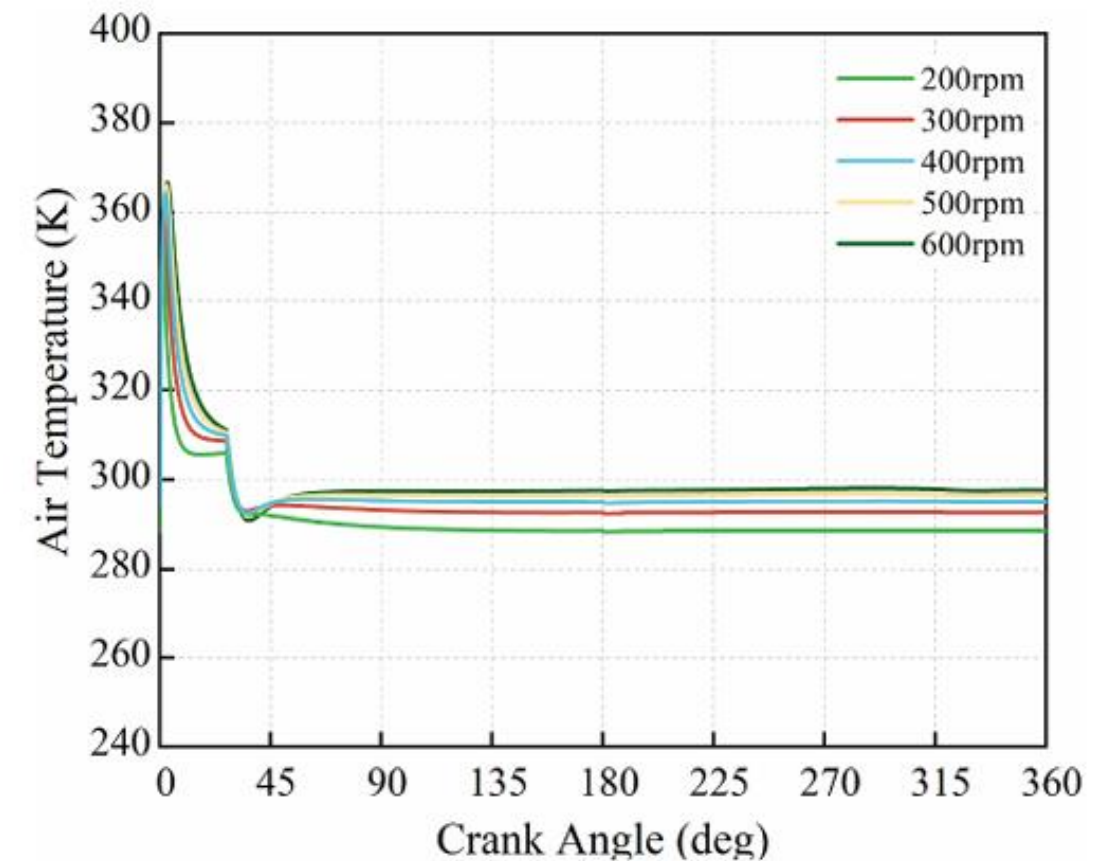
C. Qin and E. Loth, "Liquid piston compression efficiency with droplet heat transfer," Applied Energy, vol. 114, pp. 539–550, Feb. 2014.

Rotational speed vs isothermality

Gao et al. (2023) investigated the effect of low speeds in a solid piston system with water injection.

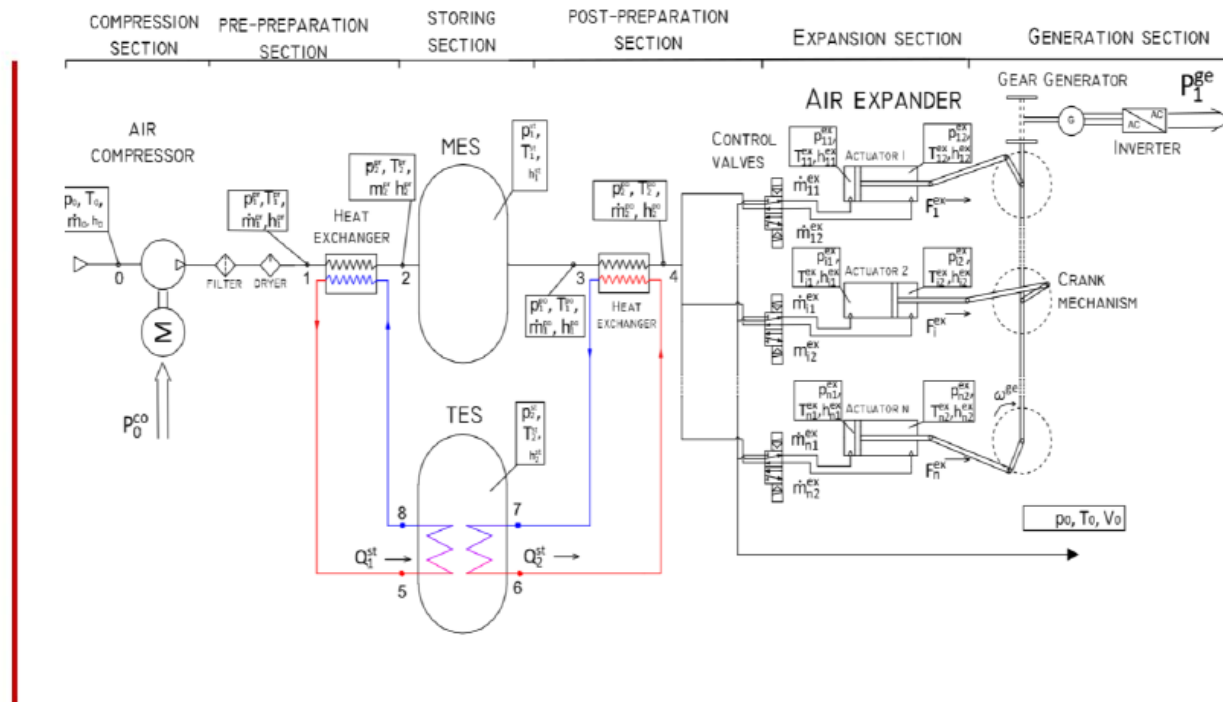
Isothermality vs. rotation speed.

Rotation speed (rpm)	Isothermality
200	75.51 %
300	75.16 %
400	73.19 %
500	69.83 %
600	64.95 %



Experimental setup

Double acting piston expander



Parameter	Value	Unit
Supply pressure p^s	5	bar
Piston diameter	50	mm
Piston stroke	500	mm
Cylinder connections size	1/2	inch
Crank length	250	mm
Cut off ratio	0.2	-
Rotational speed	20, 30, 40, 50, 60	rpm

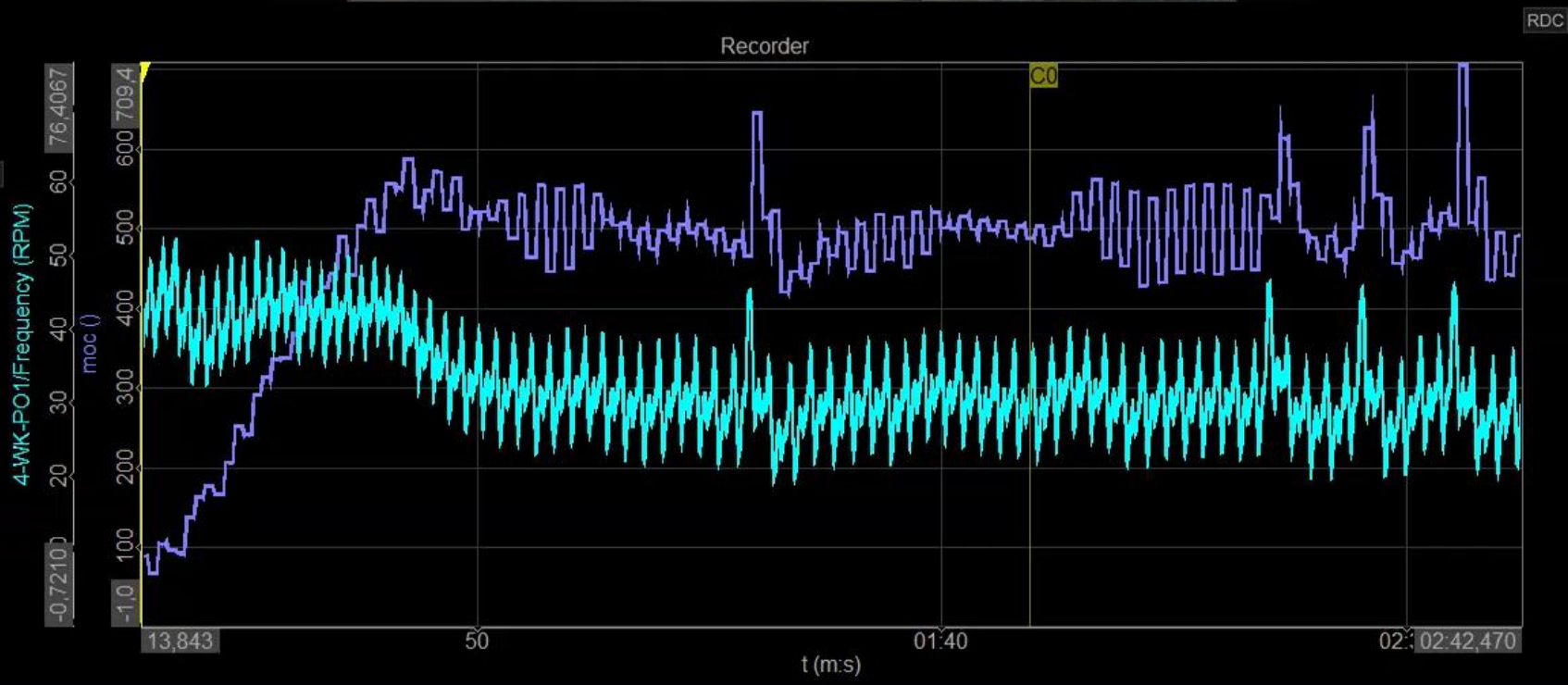
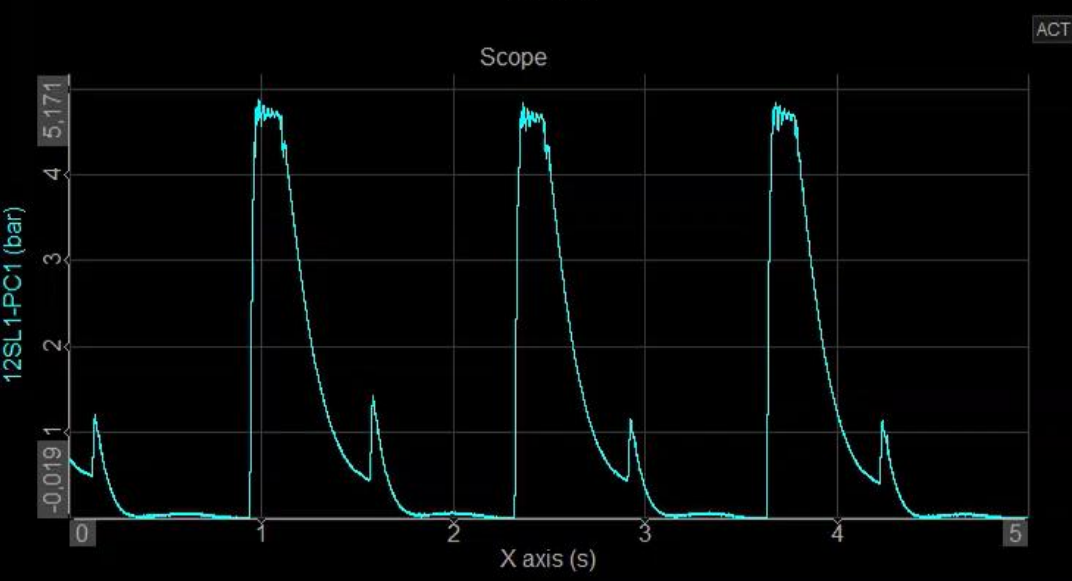
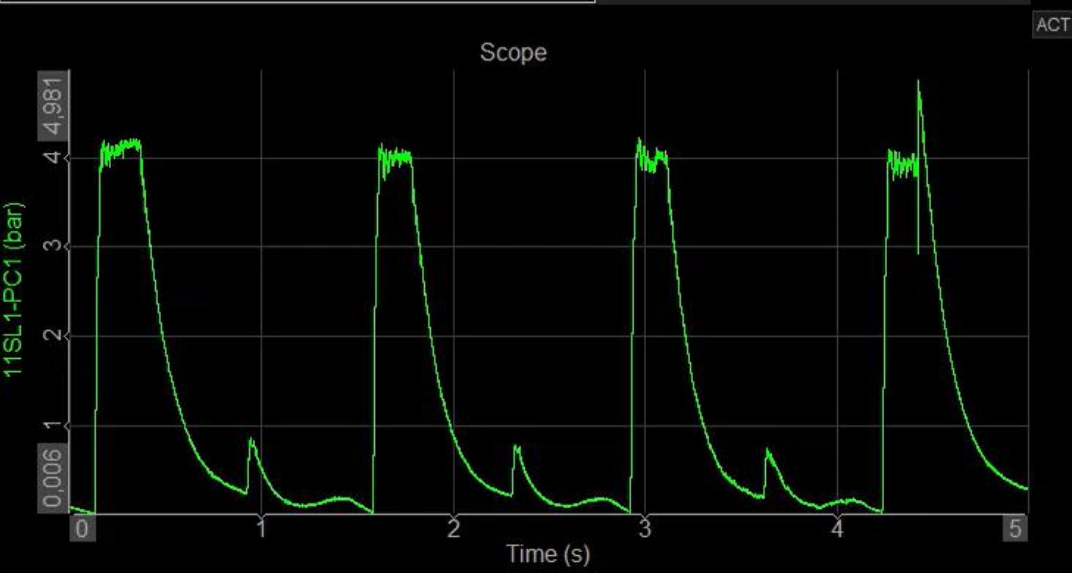
Measurement accuracy:

Pressure: $\pm 0.25\%$ FS (0–10 bar)

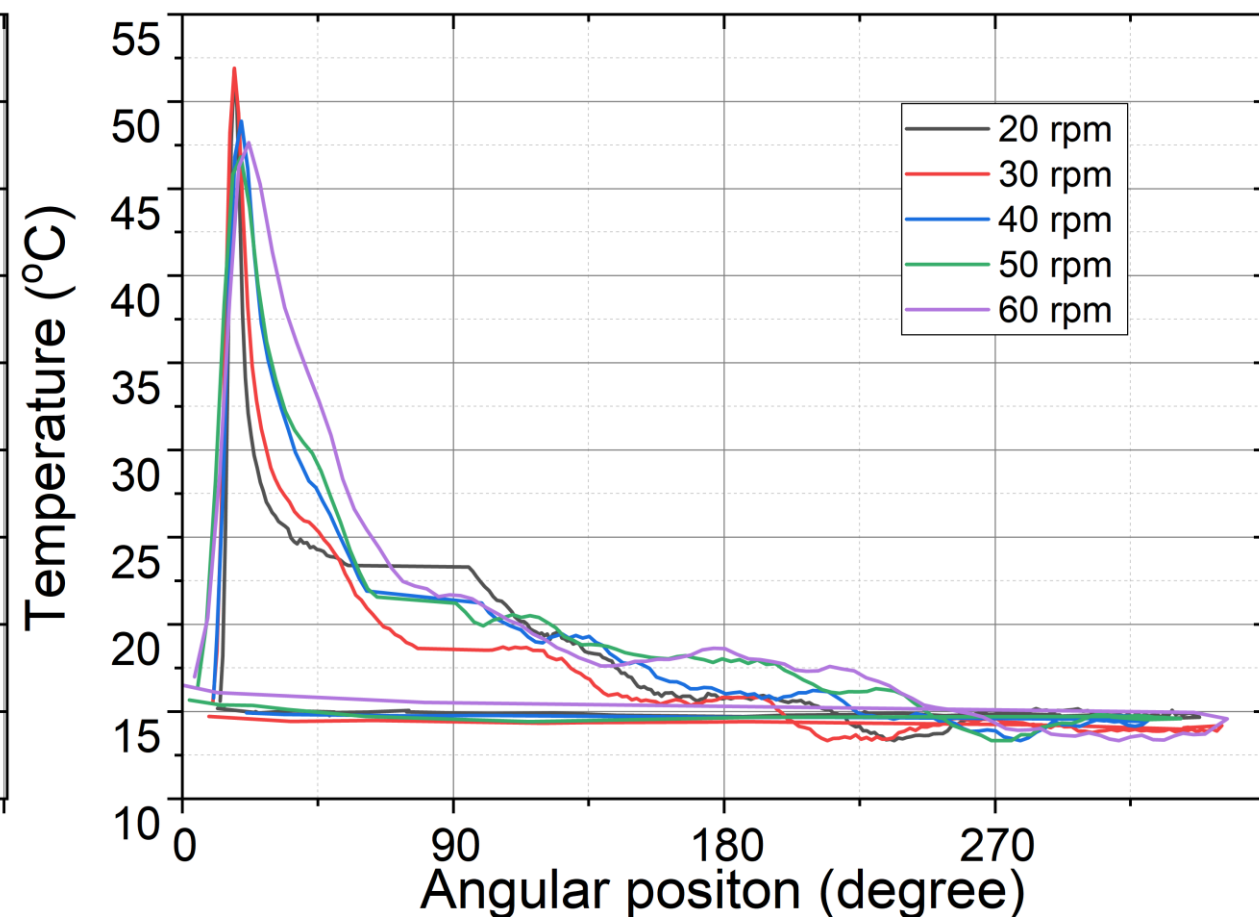
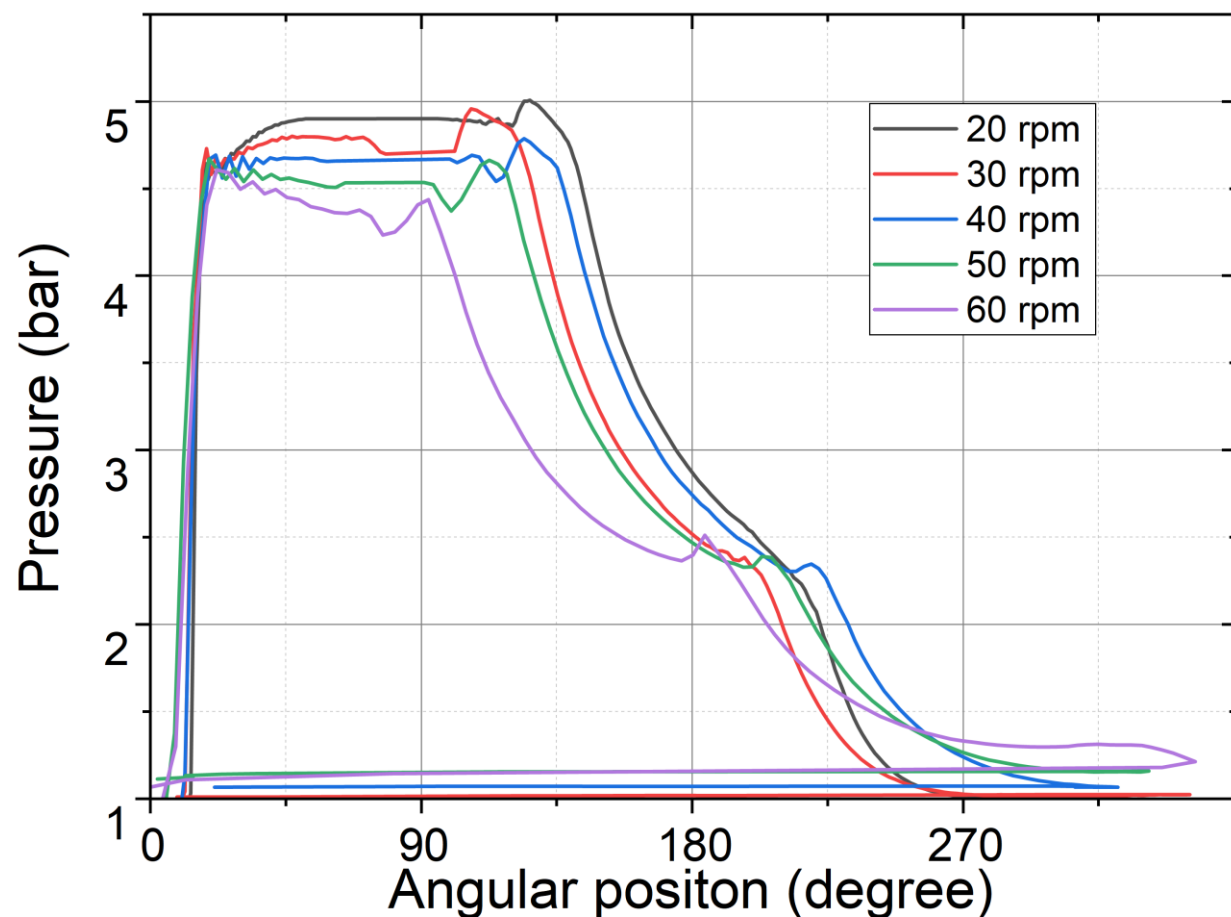
Temperature: ± 1 K

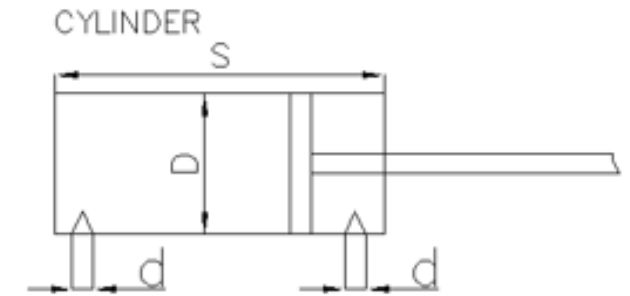
Linear position: ± 25 μ m

Angular position: 0.04°

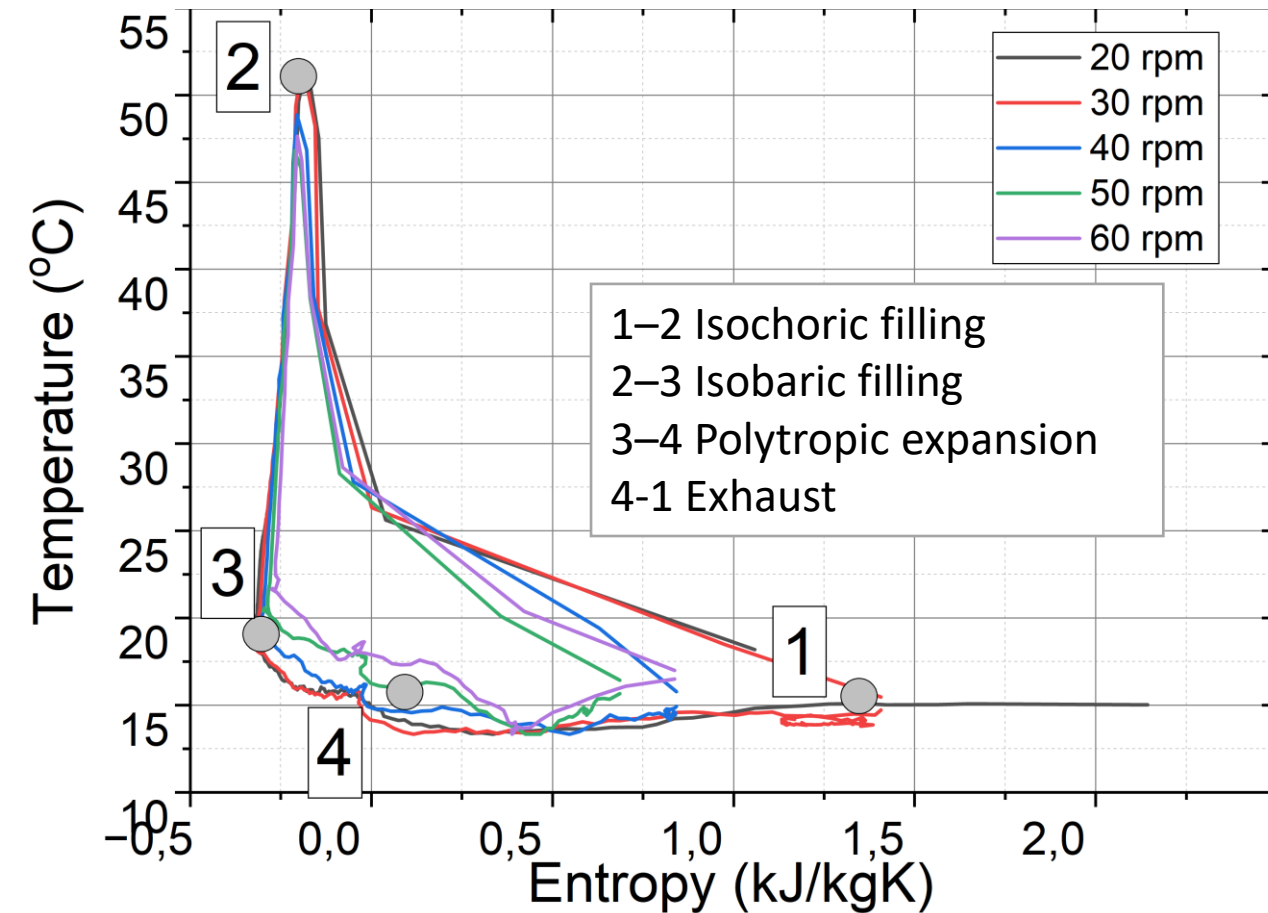
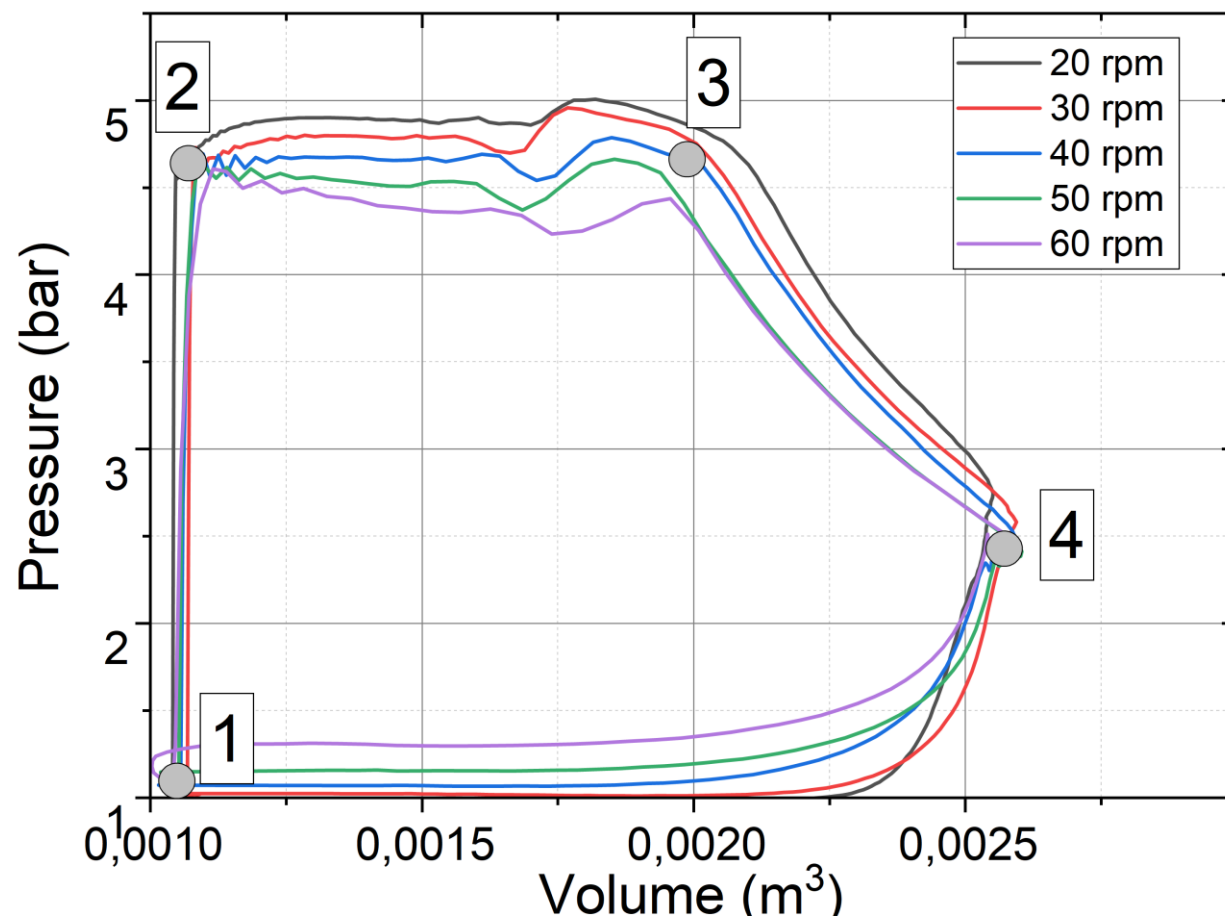


Pressure and temperature over crank angle at different piston speeds





Thermodynamic cycle (p-V and T-s) approaching near - isothermal conditions



Results

Polytropic exponent:

$$n = \frac{\ln\left(\frac{p_3}{p_4}\right)}{\ln\left(\frac{p_3}{p_4}\right) - \ln\left(\frac{T_3}{T_4}\right)}$$

p_1, p_2 – initial and final pressure of the expansion process

T_1, T_2 – initial and final temperature of the expansion process

Isothermality:

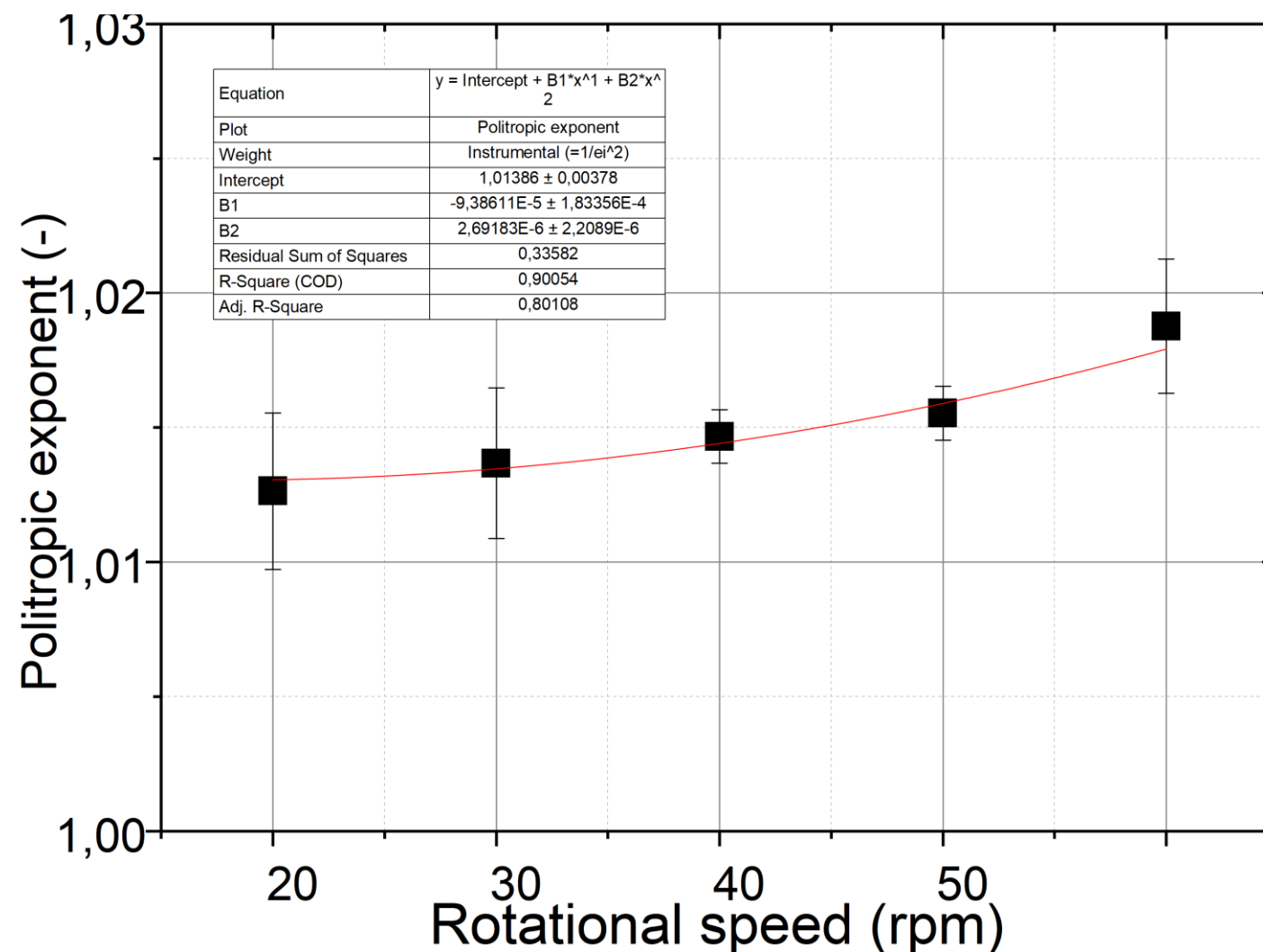
$$\phi = \frac{n - \kappa}{\kappa - 1}$$

κ – isentropic exponent – for air $\kappa = 1.4$

Results

Effect of rotational speed on the polytropic exponent and isothermal efficiency

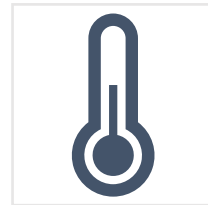
Rotational speed (rpm)	Polytropic exponent (-)	Isothermality (-)
20	1.0126	0.968
30	1.0137	0.966
40	1.0147	0.963
50	1.0155	0.961
60	1.0188	0.953



CONCLUDING REMARKS



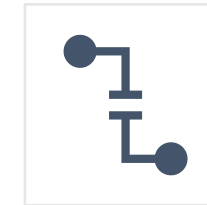
Very low piston speed regimes enable near-isothermal expansion without external heat supply



Heat transfer significantly increases at low speeds, resulting in reduced temperature gradients



The polytropic exponent approaches unity — experimentally confirmed ($n \approx 1.01$ – 1.02 for 20–60 rpm, 5-6 bar.)



Lower operating speeds correspond to larger machine dimensions, reduced power output, and higher efficiency



The results highlight the need for optimization of machine dimensions under combined criteria: power output, efficiency, and isothermality

Thank you

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